# The Strategic Under-Reporting of Bank Risk

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Motivation	Value-at-Risk	Main Tests	Model Quality	Additional Tests	
Motivat	tion				
IVIOTIVA	tion				

Risk measurement is central to financial-sector regulation.

- ► Banks are complex.
- Risk is not perfectly observable to outsiders.

Banks need to self-report their risk, which influences

- capital requirements
- market participants' risk-assessment

# This Paper

Main Questions:

- Do banks under-report their risk when they have incentives to save capital?
- What implications does this have for the risk assessment of the entire financial system?

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Empirical Setting:

- Focus on the bank's trading book.
- Banks self-report their trading book's Value-at-Risk (VaR) to the regulators.

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- Do banks under-report their risk when they have incentives to save capital?
- What implications does this have for the risk assessment of the entire financial system?

Empirical Setting:

- Focus on the bank's trading book.
- Banks self-report their trading book's Value-at-Risk (VaR) to the regulators.

The Under-Reporting Tradeoff:

Lower current capital requirement, but potentially higher future capital capital requirement. Motivation Value-at-Risk Main Tests Model Quality Additional Tests Summary

### Value-at-Risk Modeling



 Motivation
 Value-at-Risk
 Main Tests
 Model Quality
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 Summary

 Value-at-Risk
 Modeling
 Image: Comparison of Comparison of



- ► Typical trading portfolio has its largest risk exposures to:
  - interest rates
  - equities

- foreign exchange
- commodities

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 Value-at-Risk
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 Image: Comparison of Comparison of

 $W_0$ 

• Typical trading portfolio has its largest risk exposures to:

VaR

- interest rates
- equities

0.01

- foreign exchange
- commodities
- ► VaR: self-reported portfolio value-at-risk
  - level of asset holdings
  - asset volatilities

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# VaR Exceptions & Capital Charge

Capital charge =  $k \times VaR$ 

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k:

► Regulatory capital multiplier based on past year's Exceptions. *VaR Exceptions*:

► Compare reported VaR to trading book gains/losses each day.

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k:

► Regulatory capital multiplier based on past year's Exceptions. *VaR Exceptions*:

► Compare reported VaR to trading book gains/losses each day.

Exceptions	k factor	Regulatory Zone
0-4 3.00		Green
5	3.40	
6	3.50	
7	3.65	Yellow
8	3.75	
9	3.85	
10+	4.00	Red

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Data:					

▶ 15 large global banks, 2002-2012 (quarterly)

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#### Research Design

Framework for setting up empirical tests:

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$$Actual_{it} - Reported_{it} = \{G(\alpha, \Lambda_{it}, \Sigma_{realized}) - G(\alpha, \Lambda_{it}, \Sigma_{predicted})\}$$

 $+\phi(Incentives_{it}) + u_{it}$ 

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Framework for setting up empirical tests:



 $+\phi(Incentives_{it}) + u_{it}$ 

Do banks under-report their risk when their capital levels are low?

• Key incentive variable:  $Equity_{it} = \log\left(\frac{Equity}{Assets}\right)$ 

$$Exceptions_{i,t+1} = \psi(Equity)_{it} + \alpha_i + \zeta_t + \Gamma X_{it} + \epsilon_{it}$$

Prediction: Low Equity  $today \Rightarrow$  higher *future* exceptions.

• 
$$\hat{\psi} < 0$$

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• 
$$\hat{\psi} < 0$$

Note:

► The dependent variable is **Exceptions**, not VaR.

ivation Value-at-Ris	sk Main	lests IV	lodel Quality	Additional	lests
aR Exceptions	and Bo	ok Equit	ty		
	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions	(4) (z)Exceptions	(5) (z)Exceptions
(z)log(Eq/A)	$-0.70^{***}$ (0.01)				
$(z)\log(Assets)$					
(z)NI-to-Assets					
(z)Vol-Commodities					
(z)Vol-S&P 500					
(z)Vol-Foreign Exchange	е				
(z)Vol-Interest Rate					
Bank FE Year-Quarter FE	Yes Yes				
Observations 2	424				
$R^2$ Clustered by	0.45 Y-Q				

	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions	(4) (z)Exceptions	(5) (z)Exceptions
$(z)\log(Eq/A)$	$-0.70^{***}$ (0.01)	$-0.63^{***}$ (0.00)			
(z) log(Assets)		$0.51 \\ (0.16)$			
(z)NI-to-Assets		-0.03 (0.74)			
(z)Vol-Commodities					
(z)Vol-S&P 500					
(z)Vol-Foreign Exchange					
(z)Vol-Interest Rate					
Bank FE Year-Quarter FE	Yes Yes	Yes Yes			
Observations P <sup>2</sup>	424	424	-		
$R^2$ Clustered by	0.45 Y-Q	0.45 Y-Q			

	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions	(4) (z)Exceptions	(5) (z)Exceptions
$(z)\log(Eq/A)$	$-0.70^{***}$ (0.01)	$-0.63^{***}$ (0.00)	$-0.78^{***}$ (0.00)		
$(z)\log(Assets)$		$0.51 \\ (0.16)$	$0.35^{**}$ (0.02)		
(z)NI-to-Assets		-0.03 (0.74)	-0.02 (0.81)		
(z)Vol-Commodities			$0.11^{**}$ (0.03)		
(z)Vol-S&P 500			$\begin{array}{c} 0.31^{***} \\ (0.00) \end{array}$		
(z)Vol-Foreign Exchange			$   \begin{array}{c}     0.01 \\     (0.85)   \end{array} $		
(z)Vol-Interest Rate			$0.13^{**}$ (0.02)		
Bank FE Year-Quarter FE	Yes Yes	Yes Yes	Yes No		
Observations $R^2$ Clustered by	424 0.45 Y-Q	424 0.45 Y-Q	424 0.41 Y-Q		

*p*-values in parentheses \* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions	(4) (z)Exceptions	(5) (z)Exceptions
(z)log(Eq/A)	$-0.70^{***}$ (0.01)	$-0.63^{***}$ (0.00)	$-0.78^{***}$ (0.00)	$-0.66^{***}$ (0.00)	$-0.66^{**}$ (0.03)
$(z)\log(Assets)$		$0.51 \\ (0.16)$	$0.35^{**}$ (0.02)	$0.51 \\ (0.14)$	$0.51^{**}$ (0.04)
(z)NI-to-Assets		-0.03 (0.74)	-0.02 (0.81)	-0.04 (0.57)	-0.04 (0.65)
(z)Vol-Commodities			$0.11^{**}$ (0.03)	$ \begin{array}{c} 0.07 \\ (0.45) \end{array} $	$\begin{array}{c} 0.07 \\ (0.11) \end{array}$
(z)Vol-S&P 500			$\begin{array}{c} 0.31^{***} \\ (0.00) \end{array}$	$0.37^{**}$ (0.02)	$\begin{array}{c} 0.37^{**} \\ (0.03) \end{array}$
(z) Vol-Foreign Exchange			$ \begin{array}{c} 0.01 \\ (0.85) \end{array} $	$ \begin{array}{c} 0.07 \\ (0.42) \end{array} $	$\begin{array}{c} 0.07\\ (0.23) \end{array}$
(z)Vol-Interest Rate			$0.13^{**}$ (0.02)	$ \begin{array}{c} 0.07 \\ (0.70) \end{array} $	$\begin{array}{c} 0.07 \\ (0.38) \end{array}$
Bank FE Year-Quarter FE	Yes Yes	Yes Yes	Yes No	Yes Yes	Yes Yes
Observations $R^2$ Clustered by	424 0.45 Y-Q	424 0.45 Y-Q	424 0.41 Y-Q	424 0.47 Y-Q	424 0.47 Bank

*p*-values in parentheses

- $1. \ \mbox{Macro shocks cause models to perform poorly:}$
- 2. Banks have time-invariant modeling skills that affect model performance:

3. Time-varying model quality that is correlated with equity capital.

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- $1. \ \mbox{Macro shocks cause models to perform poorly:}$ 
  - Year-Quarter Fixed Effects
- 2. Banks have time-invariant modeling skills that affect model performance:
  - Bank Fixed Effects
- 3. Time-varying model quality that is correlated with equity capital.

$$Exceptions_{i,t+1} = \beta(Equity)_{it} + \alpha_i + \delta_t + \Gamma X_{it} + \epsilon_{it}$$

where

$$\begin{aligned} \epsilon_{it} &= ModelQuality_{it} + \eta_{it} \\ cov(Equity_{it}, \epsilon_{it}) &= cov(Equity_{it}, ModelQuality_{it}) \neq 0 \end{aligned}$$





## The Penalty Function and Reporting Incentives

- ► More than 4 exceptions in a year puts you in the yellow zone
- ▶ 99%-level VaR model means expectation of 0.62 exceptions/quarter.
- $\mathbb{E}[Exceptions_{4Q}] = Exceptions_{Trailing 3Q} + 0.62$

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- ► Expected-Green group: < 4 exceptions in the trailing 3 quarters.
- Expected-Yellow group  $\geq$  4 exceptions in the trailing 3 quarters.

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- ▶ 99%-level VaR model means expectation of 0.62 exceptions/quarter.
- $\mathbb{E}[Exceptions_{4Q}] = Exceptions_{Trailing 3Q} + 0.62$
- ► Expected-Green group: < 4 exceptions in the trailing 3 quarters.
- Expected-Yellow group  $\geq$  4 exceptions in the trailing 3 quarters.
- ► Key idea: Banks near the Green-Yellow threshold have
  - ► similar recent model performance, but
  - Yellow banks have stronger incentives to under-report than Green banks at the margin.





Trailing 3 Quarters Exceptions / Expected 4 Quarters Total Exceptions





Trailing 3 Quarters Exceptions / Expected 4 Quarters Total Exceptions





Trailing 3 Quarters Exceptions / Expected 4 Quarters Total Exceptions



E[·]=1

 $E[\cdot]=2 \quad E[\cdot]=3 \quad E[\cdot]=4 \quad E[\cdot]=5 \quad E[\cdot]=6 \quad E[\cdot]=7 \quad E[\cdot]=8 \quad E[\cdot]=9 \quad E[\cdot]=10$ 

Trailing 3 Quarters Exceptions / Expected 4 Quarters Total Exceptions

# The Penalty Function and Equity Capital

$$\begin{split} \textit{Exceptions}_{i,t+1} &= \beta_0 + \beta_1(\textit{NegativeEquity}_{i,t}) + \beta_2(\textit{Yellow}_{i,t}) \\ &+ \beta_3(\textit{NegativeEquity}_{i,t} \times \textit{Yellow}_{i,t}) + \Gamma X_{i,t} + \epsilon_{i,t} \end{split}$$

Identifying Assumptions for observations near the Green-Yellow Threshold:

- ► correlation between unobserved model quality and equity capital is similar.
- there are sharp changes in incentives due to changes in net benefits of under-reporting.

VaR Exceptions,	The Per	nalty Fi	unction	, and	Low Eq	uity
	(1)	(2)	(3)	(4)	(5)	(6)

	(1) Full	(2) Full	(3) Full	[0-8]	(5) [1-8]	[2-7]
(z)NegativeEquity	$\begin{array}{c} 0.75^{***} \\ (0.00) \end{array}$					
Yellow						
(z) Negative Equity * Yellow						
Red						
(z)Negative Equity * Red						
Controls	Yes					
Bank FE	Yes					
Year-Quarter FE	Yes					
Observations	378					
$\mathbb{R}^2$	0.50					
<i>p</i> -values in parentheses						
* $p < 0.10$ , ** $p < 0.05$ , *** $p < 0.05$	< 0.01					

	(1) Full	(2) Full	(3) Full	(4) [0-8]	(5) [1-8]	(6) [2-7]
(z)NegativeEquity	$0.75^{***}$ (0.00)	$0.59^{**}$ (0.02)				
Yellow		$0.54^{**}$ (0.02)				
(z) Negative Equity * Yellow						
Red		$\begin{array}{c} 0.83 \\ (0.25) \end{array}$				
(z) Negative Equity * Red						
Controls	Yes	Yes				
Bank FE	Yes	Yes				
Year-Quarter FE	Yes	Yes				
Observations	378	378				
$\mathbb{R}^2$	0.50	0.52				
<i>p</i> -values in parentheses	0.01					
p < 0.10, p < 0.05, p < 0.05, p < 0.05	: 0.01					

	(1)Full	(2) Full	(3) Full	(4) [0-8]	(5) [1-8]	(6) [2-7]
(z)NegativeEquity	$0.75^{***}$ (0.00)	$0.59^{**}$ (0.02)	$0.40^{*}$ (0.09)			
Yellow		$0.54^{**}$ (0.02)	$0.45^{*}$ (0.08)			
(z)NegativeEquity * Yellow			$0.79^{*}$ (0.06)			
Red		$     \begin{array}{c}       0.83 \\       (0.25)     \end{array} $	$\begin{array}{c} 0.54 \\ (0.34) \end{array}$			
(z)Negative Equity * Red			$\begin{array}{c} 0.37 \\ (0.24) \end{array}$			
Controls	Yes	Yes	Yes			
Bank FE	Yes	Yes	Yes			
Year-Quarter FE	Yes	Yes	Yes			
Observations	378	378	378			
$R^2$	0.50	0.52	0.55			

*p*-values in parentheses

\* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

	(1)Full	(2) Full	(3) Full	(4) [0-8]	(5) [1-8]	(6) [2-7]
(z)NegativeEquity	$0.75^{***}$ (0.00)	$0.59^{**}$ (0.02)	$0.40^{*}$ (0.09)	$0.26 \\ (0.20)$		
Yellow		$0.54^{**}$ (0.02)	$0.45^{*}$ (0.08)	$0.54^{**}$ (0.03)		
(z) Negative Equity * Yellow			$0.79^{*}$ (0.06)	$0.78^{*}$ (0.06)		
Red		$     \begin{array}{c}       0.83 \\       (0.25)     \end{array} $	$     \begin{array}{c}       0.54 \\       (0.34)     \end{array} $			
(z)Negative Equity * Red			$\begin{array}{c} 0.37 \\ (0.24) \end{array}$			
Controls	Yes	Yes	Yes	Yes		
Bank FE	Yes	Yes	Yes	Yes		
Year-Quarter FE	Yes	Yes	Yes	Yes		
Observations	378	378	378	349		
$\mathbb{R}^2$	0.50	0.52	0.55	0.58		

*p*-values in parentheses

\* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

	(1) Full	(2) Full	(3) Full	(4) [0-8]	(5) [1-8]	(6) [2-7]
(z)NegativeEquity	$0.75^{***}$ (0.00)	$0.59^{**}$ (0.02)	$0.40^{*}$ (0.09)	$ \begin{array}{c} 0.26 \\ (0.20) \end{array} $	-0.08 (0.83)	
Yellow		$0.54^{**}$ (0.02)	$0.45^{*}$ (0.08)	$0.54^{**}$ (0.03)	$0.61^{*}$ (0.05)	
(z) Negative Equity * Yellow			$0.79^{*}$ (0.06)	$0.78^{*}$ (0.06)	$1.47^{***} \\ (0.00)$	
Red		$     \begin{array}{c}       0.83 \\       (0.25)     \end{array} $	$\begin{array}{c} 0.54 \\ (0.34) \end{array}$			
(z)Negative Equity * Red			$\begin{array}{c} 0.37 \\ (0.24) \end{array}$			
Controls	Yes	Yes	Yes	Yes	Yes	
Bank FE	Yes	Yes	Yes	Yes	Yes	
Year-Quarter FE	Yes	Yes	Yes	Yes	Yes	
Observations	378	378	378	349	119	
$\mathbb{R}^2$	0.50	0.52	0.55	0.58	0.77	

*p*-values in parentheses

\* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

	(1)Full	(2) Full	(3) Full	(4) [0-8]	(5) [1-8]	(6) [2-7]
(z)NegativeEquity	$0.75^{***}$ (0.00)	$0.59^{**}$ (0.02)	$0.40^{*}$ (0.09)	$     \begin{array}{c}       0.26 \\       (0.20)     \end{array} $	-0.08 (0.83)	$1.68 \\ (0.13)$
Yellow		$0.54^{**}$ (0.02)	$0.45^{*}$ (0.08)	$0.54^{**}$ (0.03)	$0.61^{*}$ (0.05)	1.01 (0.38)
(z)NegativeEquity * Yellow			$0.79^{*}$ (0.06)	$0.78^{*}$ (0.06)	$\begin{array}{c} 1.47^{***} \\ (0.00) \end{array}$	$\frac{1.54^{**}}{(0.04)}$
Red		$ \begin{array}{c} 0.83 \\ (0.25) \end{array} $	$ \begin{array}{c} 0.54 \\ (0.34) \end{array} $			
(z)Negative Equity * Red			$ \begin{array}{c} 0.37 \\ (0.24) \end{array} $			
Controls Bank FE Year-Quarter FE	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes
$\frac{\text{Observations}}{R^2}$	$378 \\ 0.50$	$378 \\ 0.52$	$378 \\ 0.55$	$349 \\ 0.58$	$\begin{array}{c} 119 \\ 0.77 \end{array}$	$\frac{64}{0.85}$

*p*-values in parentheses

\* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

#### Stale Model Unrelated to Incentives

- ► Banks were just too slow to update their model.
- ► Failure to update the model is unrelated to incentives.

Two Additional Tests:

- 1. leave out the transition period
- 2. exploit the dynamics of exceptions

#### Stale Model Unrelated to Incentives

- ► Banks were just too slow to update their model.
- ► Failure to update the model is unrelated to incentives.

Two Additional Tests:

- 1. leave out the transition period
- 2. exploit the dynamics of exceptions
  - ► Use lagged exception as a proxy for time-varying modeling skill:

*Exceptions*<sub>*i*,*t*+1</sub> =  $\beta$ (*Equity*)<sub>*i*t</sub> +  $\alpha_i$  +  $\delta_t$  +  $\Gamma X_{it}$  +  $\theta Exceptions_{i,t}$  +  $\eta_{it}$ 

#### Stale Model Tests

Motivation	Value-at-Risk	Main Tests	Model Quality	Additional Tests	
Stale M	odel Tests				

	(1) All	(3) AB1lag	(4) AB2lags
$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)		
L.(z)Exceptions			
L2.(z)Exceptions			
Controls	Yes		
Bank FE	Yes		
Year-Quarter FE	Yes		
Observations	424		
$R^2$	0.47		
2nd Order AR test <i>p</i> -value			
Sargan Test $p$ -value			
<i>p</i> -values in parentheses			
* $p < 0.10$ , ** $p < 0.05$ , *** $p < 0$	0.01		

Motivation	Value-at-Risk	Main Tests	Model Quality	Additional Tests	
Stale M	odel Tests				

	(1) All		(3) AB1lag	(4) AB2lags
$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)	$-0.65^{**}$ (0.01)		
L.(z)Exceptions				
L2.(z)Exceptions				
Controls	Yes	Yes		
Bank FE Year-Quarter FE	Yes Yes	Yes Yes		
Observations 72	424	379		
$K^2$ 2nd Order AR test <i>p</i> -value Sargan Test <i>p</i> -value	0.47	0.48		
<i>p</i> -values in parentheses				

Motivation	Value-at-Risk	Main Tests	Model Quality	Additional Tests	

#### Stale Model Tests

	(1) All	(2) drop2007	(3) AB1lag	(4) AB2lags
$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)	$-0.65^{**}$ (0.01)	$-0.45^{**}$ (0.01)	
L.(z)Exceptions			$0.30^{***}$ (0.00)	
L2.(z)Exceptions				
Controls Bank FE Year-Quarter FE	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes	
$\begin{array}{c} \mbox{Observations}\\ R^2\\ \mbox{2nd Order AR test $p$-value}\\ \mbox{Sargan Test $p$-value} \end{array}$	424 0.47	379 0.48	392 0.94 0.49	-

Motivation	Value-at-Risk	Main Tests	Model Quality	Additional Tests	

Stale	Model	Tests
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	(1) All	$\binom{(2)}{\text{drop2007}}$	(3) AB1lag	(4) AB2lags
$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)	$-0.65^{**}$ (0.01)	$-0.45^{**}$ (0.01)	$-0.47^{**}$ (0.02)
L.(z)Exceptions			$0.30^{***}$ (0.00)	$\begin{array}{c} 0.31^{***} \\ (0.00) \end{array}$
L2.(z)Exceptions				-0.01 (0.96)
Controls	Yes	Yes	Yes	Yes
Bank FE	Yes	Yes	Yes	Yes
Year-Quarter FE	Yes	Yes	Yes	Yes
Observations	424	379	392	378
$R^2$	0.47	0.48		
2nd Order AR test <i>p</i> -value			0.94	1.00
Sargan Test <i>p</i> -value			0.49	0.52

*p*-values in parentheses \* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

### Variation in the Benefits of Under-Reporting

Cross-Sectional Variation:

Banks with large trading operations.

Time Series Variation:

• Times when the financial system is under stress.

Key idea: Under-reporting provides more capital relief to banks with relatively larger trading desks.

Key idea: Under-reporting provides more capital relief to banks with relatively larger trading desks.

Measure: VaR-to-equity-capital ratio as of 2006Q1 (VE\_2006).

- ► Captures the relative importance of VaR levels to capital charges.
- Freezing the measure at 2006Q1 ensures it is not affected by post-crisis changes in risk-taking behavior or equity capital.

*Exceptions*<sub>*i*,*t*+1</sub> =  $\psi$ (*Equity*)<sub>*i*t</sub> +  $\theta$ (*Equity*<sub>*i*t</sub> × *VE*\_2006<sub>*i*</sub>) +  $\Gamma$ X<sub>*i*t</sub> +  $\epsilon$ <sub>*i*t</sub>

Prediction: Larger Trading Exposure  $\Rightarrow$  higher sensitivity to low capital.  $\blacktriangleright \ \hat{\theta} < 0$ 

	(1) $(z)Exceptions$	(2) (z)Exceptions	(3) (z)Exceptions
$(z)\log(Eq/A)$	$-0.92^{**}$ (0.01)		
(z) VE_2006 * (z) log(Eq/A)			
High (VE_2006) * (z)log (Eq/A)			
Controls	Yes		
Bank FE	Yes		
Year-Quarter FE	Yes	_	
Observations	330	-	
$R^2$	0.47		
<i>p</i> -values in parentheses		•	

	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions
$(z)\log(Eq/A)$	$-0.92^{**}$ (0.01)	-0.50 (0.15)	
(z)VE_2006 * (z)log(Eq/A)		$-0.48^{**}$ (0.02)	
High(VE_2006) * (z)log(Eq/A)			
Controls	Yes	Yes	
Bank FE	Yes	Yes	
Year-Quarter FE	Yes	Yes	
Observations	330	330	
$R^2$	0.47	0.50	

p-values in parentheses

	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions
$(z)\log(Eq/A)$	$-0.92^{**}$ (0.01)	-0.50 (0.15)	$0.35 \\ (0.45)$
(z) VE_2006 * (z) log(Eq/A)		$-0.48^{**}$ (0.02)	
High(VE_2006) * (z)log(Eq/A)			$^{-1.92^{**}}_{(0.02)}$
Controls	Yes	Yes	Yes
Bank FE	Yes	Yes	Yes
Year-Quarter FE	Yes	Yes	Yes
Observations	330	330	330
$R^2$	0.47	0.50	0.51

 $p\mbox{-}v\mbox{alues}$  in parentheses

During times of financial sector stress:

- capital is likely most costly
- it is most important for regulators to get an accurate measurement of risk
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During times of financial sector stress:

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- $\Rightarrow$  Both private benefits and social costs of under-reporting are high.

We focus on two main proxies of system-wide stress:

- 1. Lehman Brothers' collapse (2008Q4)
- 2. V-lab Capital Shortfall measure (Acharya et al. 2010)

$$Exceptions_{i,t+1} = \psi(Equity)_{it} + \rho(Stress)_t \\ + \phi(Equity_{it} * Stress_t) + \Gamma X_{it} + \epsilon_{it}$$

	(1) $(z)Exceptions$	(2) (z)Exceptions	(3) (z)Exceptions	(4) (z)Exceptions
$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)			
(z)log(Eq/A) * 2008q4				
HiMES (top 4-tile)				
(z)log(Eq/A) * HiMES				
Controls	Yes			
Bank FE	Yes			
Year-Quarter FE	Yes			
Observations	424	_		
$R^2$	0.47			
<i>p</i> -values in parentheses * $p < 0.10$ , ** $p < 0.05$ , ***	p < 0.01	-		

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$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)	$-0.57^{**}$ (0.01)		
(z)log(Eq/A) * 2008q4		$-1.75^{***}$ (0.00)		
HiMES (top 4-tile)				
(z)log(Eq/A) * HiMES				
Controls	Yes	Yes		
Bank FE	Yes	Yes		
Year-Quarter FE	Yes	Yes		
Observations	424	424		
$\mathbb{R}^2$	0.47	0.56		
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	(1) (z)Exceptions	(2) (z)Exceptions	(3) (z)Exceptions	(4) (z)Exceptions	
$(z)\log(Eq/A)$	$-0.66^{***}$ (0.00)	$-0.57^{**}$ (0.01)	$-0.66^{***}$ $(0.01)$	-0.26 (0.18)	
(z)log(Eq/A) * 2008q4		(0.00)			
HiMES (top 4-tile)			$   \begin{array}{c}     0.22 \\     (0.56)   \end{array} $	$\begin{array}{c} 0.21 \\ (0.57) \end{array}$	
(z)log(Eq/A) * HiMES				$-0.42^{**}$ (0.04)	
Controls	Yes	Yes	Yes	Yes	
Bank FE	Yes	Yes	Yes	Yes	
Year-Quarter FE	Yes	Yes	Yes	Yes	
Observations	424	424	424	424	
$R^2$	0.47	0.56	0.48	0.51	

*p*-values in parentheses \* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

Additional Robustness Tests:

- 1. Alternative measures of capital.
- 2. Poisson/negative binomial specifications.
- 3. Alternative measure of "excess" exceptions.
- 4. Control for
  - time-varying market risk exposure.
  - time-varying MBS exposure.
  - time-varying VaR risk factor exposure.

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The Level of VaR and Equity Capital:

- Prior volatility directly maps to the level of VaR.
- ► We find the a weaker relationship between past market volatility and reported level of VaR when firms have lower equity capital.
  - Suggests firms are using more discretion in the VaR reports when undercapitalized.

Motivation Value-at-Risk Main Tests Model Quality Additional Tests Summary
Summary

- Proper risk measurement is critical for the stability of individual financial institution and the financial system at large.
  - Important for within-firm capital allocation decisions and risk management.
  - ► Important for regulators to ensure a stable, functioning financial sector.
- The system provides managers with the incentives and ability to under-report risk to save capital when raising capital is more costly.

 $\Rightarrow$  The states of the world when accurate risk measurement may be most important are precisely when this measurement is least informative.

### The Strategic Under-Reporting of Bank Risk

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<sup>2</sup>University of Michigan

<sup>3</sup>Northeastern University

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### **Descriptive Statistics**

	Mean	$^{\mathrm{SD}}$	Min	P25	Median	P75	Max	Ν
Bank Characteristics:								
Total Assets (\$Bn)	901.40	767.93	73.14	291.14	602.46	1428.16	3643.58	424
NI-to-Assets (%,Q)	0.17	0.20	-1.16	0.09	0.18	0.25	1.57	424
BookEq/AT (%)	6.32	3.15	1.69	4.06	5.14	9.01	13.84	424
$\log(Eq/AT)$	-2.89	0.51	-4.08	-3.20	-2.97	-2.41	-1.98	424
Value-at-Risk (\$MM):								
Exceptions	0.62	2.00	0.00	0.00	0.00	0.00	13.00	424
Total Value-at-Risk	61.90	85.86	3.60	9.00	26.00	75.00	433.00	422
VaR-Interest Rate	46.42	73.39	0.00	4.40	15.28	60.80	430.58	422
VaR-Foreign Exchange	9.09	12.44	0.00	0.89	2.69	15.70	62.82	422
VaR-Equities	20.87	31.39	0.00	3.14	7.64	27.12	204.60	422
VaR-Commodities	7.49	10.80	0.00	0.29	2.08	10.50	52.31	422
VaR-Other	17.23	49.72	0.00	0.00	0.00	8.65	322.88	422
VaR-Diversification Benefit	40.89	54.01	0.00	4.86	11.70	59.60	241.67	422

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